

## IV. CONCLUSION

The simple temperature compensated oscillator has been designed for use with avalanche transit time diodes. A ceramic capacitor which has a negative temperature coefficient is used for a temperature compensator. Stabilized oscillators are improved considerably in performance compared with nonstabilized oscillators of the same cavity.

The frequency drift in the low- $Q$  cavity having parallel ceramic capacitor with the diode package is less than  $+30$  kHz/ $^{\circ}\text{C}$ . These compensation techniques need no additional structures such as a

stabilized cavity and a mechanical compensating tuner. Especially, simplicity, low cost, and compact size are the main advantages of employing the ceramic loading on the diode package to compensate for temperature changes. Moreover, since this technique is completely passive, no power is required and the frequency stability shows the same results as the mechanical tuning compensation.

## REFERENCES

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## Letters

## Comments on "Rectangular Waveguides with Impedance Walls"

P. R. McISAAC

In the above paper,<sup>1</sup> Dybal *et al.* discuss the propagation characteristics of several rectangular waveguides with corrugated walls and analyze them by using impedance boundaries to simulate the corrugated walls. One of the waveguides discussed, called an *E* guide, has longitudinal corrugations in all four walls. The authors claim that this waveguide will support *E* modes but not *H* modes. However, this waveguide has an isotropic homogeneous dielectric surrounded by a conducting boundary which is longitudinally uniform. Therefore, if the boundary is assumed to be a perfect conductor, this waveguide must support a complete set of both *E* and *H* modes; the presence of the corrugations cannot change this conclusion.

In their discussion of the *E* guide in Section III,<sup>1</sup> the authors state that the wall impedances  $Z_2 = Z_3 = 0$ ,  $Z_1 \neq 0$ ,  $Z_4 \neq 0$  (refer to their paper for the definitions of these impedances) may be used to simulate a rectangular waveguide with longitudinally corrugated walls. They assert as follows.

"The ordinary *E* modes satisfy the impedance boundary conditions for this impedance configuration while the *H* modes do not."

They also assert the following.

"Modal solutions other than *E* modes have field components that are incompatible with the impedance boundary conditions." No proof is offered for these assertions.

In fact, these assertions are not correct. Consider the following set of electromagnetic field components in the region:  $-W/2 < x < W/2$ ,  $-H/2 < y < H/2$  (for convenience, the origin of the coordinate system is shifted to the center of the waveguide, see Fig. 1<sup>1</sup>). The notation is essentially that used in the original paper.<sup>1</sup>

$$E_x = \frac{-j\omega\mu}{\Gamma^2 + k^2} K_y H_0 \sin(K_x x) \cos(K_y y) \exp(-\Gamma z)$$

$$E_y = \frac{j\omega\mu}{\Gamma^2 + k^2} K_x H_0 \cos(K_x x) \sin(K_y y) \exp(-\Gamma z)$$

$$E_z = 0$$

$$H_x = \frac{-\Gamma}{\Gamma^2 + k^2} K_x H_0 \cos(K_x x) \sin(K_y y) \exp(-\Gamma z)$$

$$H_y = \frac{-\Gamma}{\Gamma^2 + k^2} K_y H_0 \sin(K_x x) \cos(K_y y) \exp(-\Gamma z)$$

$$H_z = H_0 \sin(K_x x) \sin(K_y y) \exp(-\Gamma z).$$

It is easily verified that these field components satisfy all of Maxwell's equations if

$$\Gamma^2 + k^2 - K_x^2 - K_y^2 = 0.$$

In addition, this set of field components is compatible with the impedance conditions at the walls stated by the authors. Assuming that the nonzero wall impedances are reactive, so that  $Z_1 = jX_1$  and  $Z_4 = jX_4$ , the boundary conditions at the walls are

$$jX_1 = \frac{-E_x(x, H/2)}{H_z(x, H/2)}, \quad \text{at } y = H/2$$

$$jX_4 = \frac{E_y(W/2, y)}{H_z(W/2, y)}, \quad \text{at } x = W/2$$

with analogous expressions at the other walls.

Inserting the field components given above into these boundary conditions, one obtains

$$(K_y H/2) \cot(K_y H/2) = \frac{\Gamma^2 + k^2}{k^2} \frac{kH}{2} \frac{X_1}{Z_0}$$

$$(K_x W/2) \cot(K_x W/2) = \frac{\Gamma^2 + k^2}{k^2} \frac{kW}{2} \frac{X_4}{Z_0}.$$

This pair of equations, together with

$$\Gamma^2 + k^2 - K_x^2 - K_y^2 = 0$$

are sufficient to determine the  $k$  versus  $\Gamma$  relationship for given values of  $H$ ,  $W$ ,  $X_1$ , and  $X_4$ .

There are an infinite set of solutions to the pair of transcendental equations just given. In addition to these solutions, there are three other infinite sets of solutions that can be obtained, based on

$$H_z = H_0 \sin(K_x x) \cos(K_y y) \exp(-\Gamma z)$$

$$H_z = H_0 \cos(K_x x) \sin(K_y y) \exp(-\Gamma z)$$

$$H_z = H_0 \cos(K_x x) \cos(K_y y) \exp(-\Gamma z)$$

respectively. Therefore, contrary to the assertion made in the paper,<sup>1</sup> the impedance wall model used there has an infinite set of *H* modes.

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The author is with the Department of Electrical Engineering, Cornell University, Ithaca, N. Y. 14850.

<sup>1</sup> R. B. Dybal, L. Peters, Jr., and W. H. Peake, *IEEE Trans. Microwave Theory Tech.*, vol. MTT-19, pp. 2-9, Jan 1971.

The exact location of the cutoff frequencies of these  $H$  modes will, of course, depend on  $H$  and  $W$ , and on the sign, magnitude, and frequency dependence of  $X_1$  and  $X_4$ . For the case of a symmetric square waveguide ( $H = W$ ,  $X_4 = X_1$ ), it can be shown that the cutoff frequency of the lowest  $H$  mode is *always* below that of the  $E_{11}$  mode. At cutoff,  $\Gamma = 0$  and  $k = k_c = (K_x^2 + K_y^2)^{1/2}$ . If  $X_4 = X_1$  is positive (inductive reactance) the lowest  $H$  mode (for which  $K_y = K_x$ ) is associated with  $H_z = H_0 \sin(K_x x) \sin(K_y y) \exp(-\Gamma z)$  and has a normalized cutoff frequency

$$k_c W = 2\sqrt{2} \cot^{-1}(\sqrt{2}X_1/Z_0).$$

The first solution of this equation is always less than  $\sqrt{2}\pi$ , the value of the normalized cutoff frequency of the  $E_{11}$  mode. If  $X_4 = X_1$  is negative (capacitive reactance) the lowest  $H$  mode ( $K_y = K_x$ ) is associated with  $H_z = H_0 \cos(K_x x) \cos(K_y y) \exp(-\Gamma z)$  and has a normalized cutoff frequency

$$k_c W = 2\sqrt{2} \tan^{-1}(-\sqrt{2}X_1/Z_0).$$

Again, the first solution of this equation (recall that  $-X_1$  is positive), is always less than  $\sqrt{2}\pi$ , the value for the  $E_{11}$  mode. Thus, based on this model, an  $H$  mode will always be the dominant mode of the waveguide, and the  $E_{11}$  mode can never be the dominant mode.

In their paper,<sup>1</sup> the authors state that in an experimental study of a square waveguide with longitudinally corrugated walls, they found no evidence of any  $H$  modes over a two-to-one frequency range which included the cutoff frequency of the  $E_{11}$  mode. They concluded that the  $E_{11}$  mode was the dominant mode of the waveguide. The fact that these experimental results conflict with the results of a correct analysis of the wall impedance model suggests that a critical reexamination of the whole problem should be undertaken to resolve this conflict. In view of this conflict, acceptance of the authors' contention that a longitudinally corrugated waveguide always has a dominant  $E$  mode appears inadvisable until an independent confirmation of their experimental results is available.

modes will be limited to three only. This can be explained physically also by observing that given the polarization for a desired mode of operation (viz., TE to  $x$  or TE to  $y$ ) only one pair of walls will act as an anisotropic surface and the other (with corrugations parallel to the  $E$  field) will act only as a conducting surface [4]. This observation has been made by Dybdal *et al.* also.<sup>1</sup> Further considering the modal solution corresponding to the TE to  $x$  mode within the corrugated guide of this type one observes that  $E_x = 0$  everywhere,  $E_y = 0$ , and  $E_z = 0$  on the  $H$  walls [2]. Hence  $Z_1 = Z_3 = Z_4 = 0$  and  $Z_2 \neq 0$ , which satisfy (1). Recently it has been confirmed experimentally [4] that a waveguide with all the four walls corrugated transversely gives satisfactory results when it is excited in TE to  $x$  or TE to  $y$  mode. This has also been verified by us by constructing a square corrugated guide. Similarly, when the corrugated guide is excited in the TE to  $y$  mode  $Z_1 = Z_2 = Z_4 = 0$  and  $Z_3 \neq 0$ . Again (1) is satisfied. For this mode of operation the  $E$ -plane corrugated surface behaves like a conducting surface and the  $H$ -plane walls are anisotropic. From the previous discussions it is obvious that the corrugated surface can behave as an anisotropic as well as an isotropic surface, depending upon the choice of the mode of excitation used. From these observations the authors believe that the square corrugated guide may be used most efficiently as a wideband dual polarized device by a judicious choice of the corrugation depth.

## REFERENCES

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## Comments on "Rectangular Waveguides with Impedance Walls"

M. S. NARASIMHAN AND V. VENKATESWARA RAO

In the above paper,<sup>1</sup> some comments seem to be necessary on the impedance compatibility relation

$$Z_1 Z_3 - Z_2 Z_3 + Z_2 Z_4 = 0 \quad (1)$$

where  $Z_1$ ,  $Z_2$ ,  $Z_3$ , and  $Z_4$  have been defined.<sup>1</sup> This relation was derived for obtaining a separable modal solution of fields. Though (1) appears to be mathematically correct, controversies arise when it is used for square or rectangular waveguides with all the four walls corrugated transversely to the direction of propagation. Bryant [1] in his analysis used a square corrugated waveguide excited in the TE to  $x$  mode of operation and observed that the  $H$ -plane walls, though corrugated, will act as a conducting surface and will not affect the propagation of TE to  $x$  modes. Dybdal *et al.* have pointed out that for this particular geometry (1) is not satisfied and in order to satisfy (1) the  $H$ -plane walls should be conducting. We would like to point out that it is well known that a separable modal solution of fields in a waveguide with impedance walls may be expressed in terms of

$$\left\{ \begin{array}{l} \text{TE} \\ \text{TM} \end{array} \right\} \text{ to } x \quad \text{or} \quad \left\{ \begin{array}{l} \text{TE} \\ \text{TM} \end{array} \right\} \text{ to } y \text{ modes [3].}$$

Hence the impedances which can influence the propagation of these

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The authors are with the Department of Electrical Engineering, Indian Institute of Technology, Madras, India.

<sup>1</sup> R. B. Dybdal, L. Peters, Jr., and W. H. Peake, *IEEE Trans. Microwave Theory Tech.*, vol. MTT-19, pp. 2-9, Jan. 1971.

## Surface Acoustic Wave Properties of Tantalum Pentoxide Thin Films on YX Quartz

J. F. WELLER AND T. G. GIALLORENZI

**Abstract**—The properties of a Rayleigh surface wave propagating in tantalum oxide thin films on YX quartz are presented. Dispersion and acoustic wave loss measurements are made using the optical probe technique.

The propagation characteristics of surface acoustic waves (SAW) in layered structures differ in several ways from those on a free surface. Rayleigh waves on a free surface are normally dispersionless and have low losses for frequencies less than 300 MHz ( $\leq 1$  dB/cm in YX quartz). The introduction of a thin film causes velocity dispersion [1] as well as an increase in the losses of the SAW. The film can either mass load the surface which slows the SAW or effectively strengthen the elastic properties of the surface which increases the velocity. In the latter case the wave velocity increases to the point where the wave becomes leaky, i.e., when it has a phase velocity equal to that of the lowest transverse bulk wave; eventually at large film thicknesses, mass loading will again predominate and the wave slows down. Finally, the film introduces more loss due to increased scattering caused by grain boundaries and other surface imperfections [2] and by step discontinuities as recently discussed by Munasinghe and Farnell [3].

The introduction of velocity dispersion resulting from a thin film overlay leads to several applications for SAW devices. Mass loading can be used to produce acoustical waveguiding and provides a means for steering, focusing, or defocusing the SAW [2]. In a few cases where the thin film causes an increase in the phase velocity,

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The authors are with the Optical Sciences Division, Naval Research Laboratory, Washington, D.C. 20375.